

# Conformal or Confining

Elisabetta Pallante  
U. of Groningen  
The Netherlands



rijksuniversiteit  
 groningen

faculteit wiskunde en  
 natuurwetenschappen

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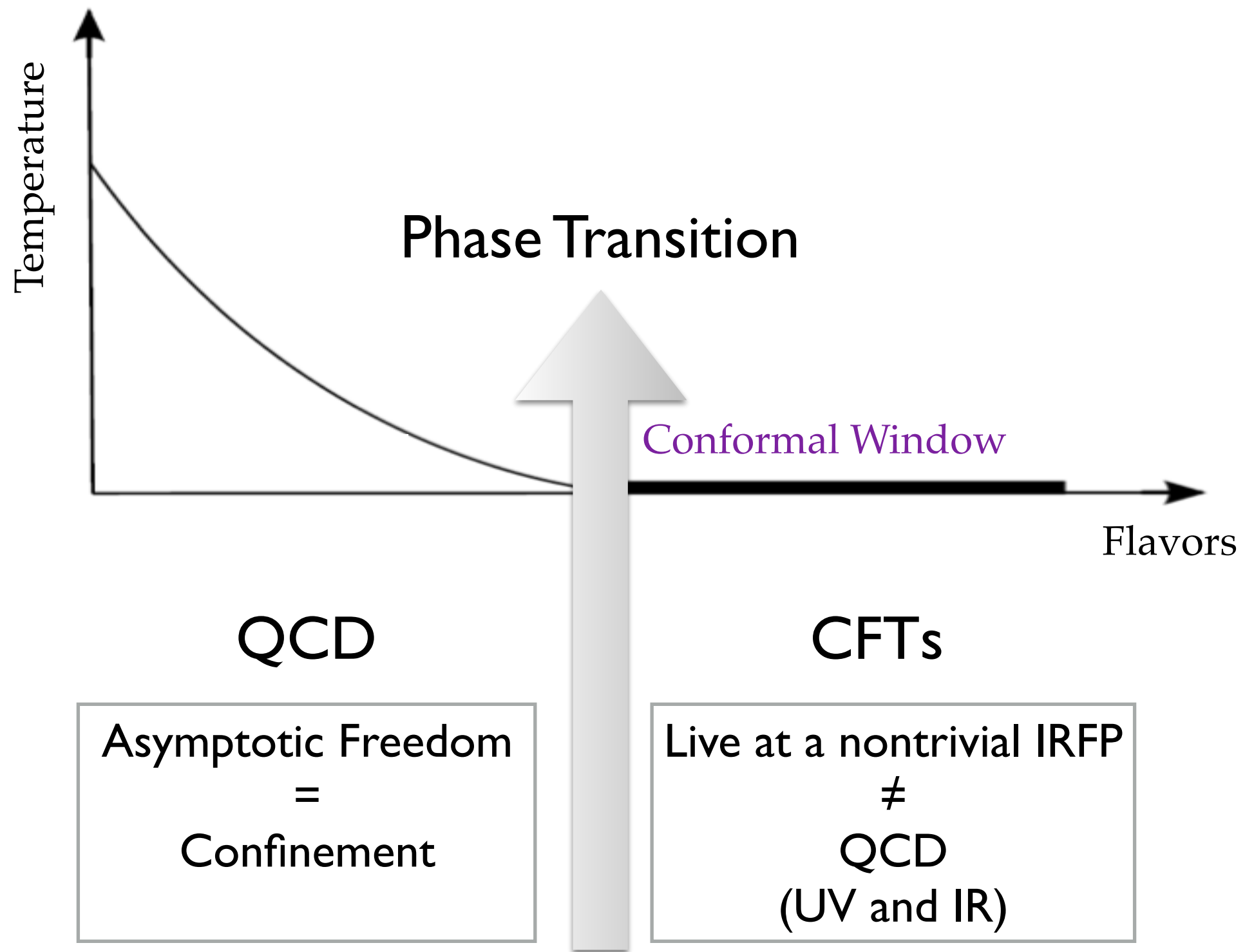


# Outline

BASED ON NUNES DA SILVA, EP, ROBROEK ARXIV:1506.06396

Given Yang-Mills plus  $N_f$  massless flavors (any representation)

- ▶ Question: How far is the complete theory from perturbation theory or large- $N$  ?
  - I) Interplay of confinement and chiral symmetry
  - II) Consequences of removing supersymmetry
- ▶ Numerical study of the lower edge of the CW
- ▶ Theoretical analysis of the scalar glueball anomalous dimension



VERY RELEVANT RESULT  
[ BOCHICCHIO NPB875 2013 ]

## Question

How far is the complete theory from  
perturbation theory or large- $N$  ?

Lattice study

One step towards the answer:

Identify the lower edge of the CW with a lattice formulation of the theory (Euclidean action for YM+N<sub>f</sub>)

Strategy:

Use observable(s) that undergo a phase transition — other observables are likely to change smoothly across the endpoint

This study:

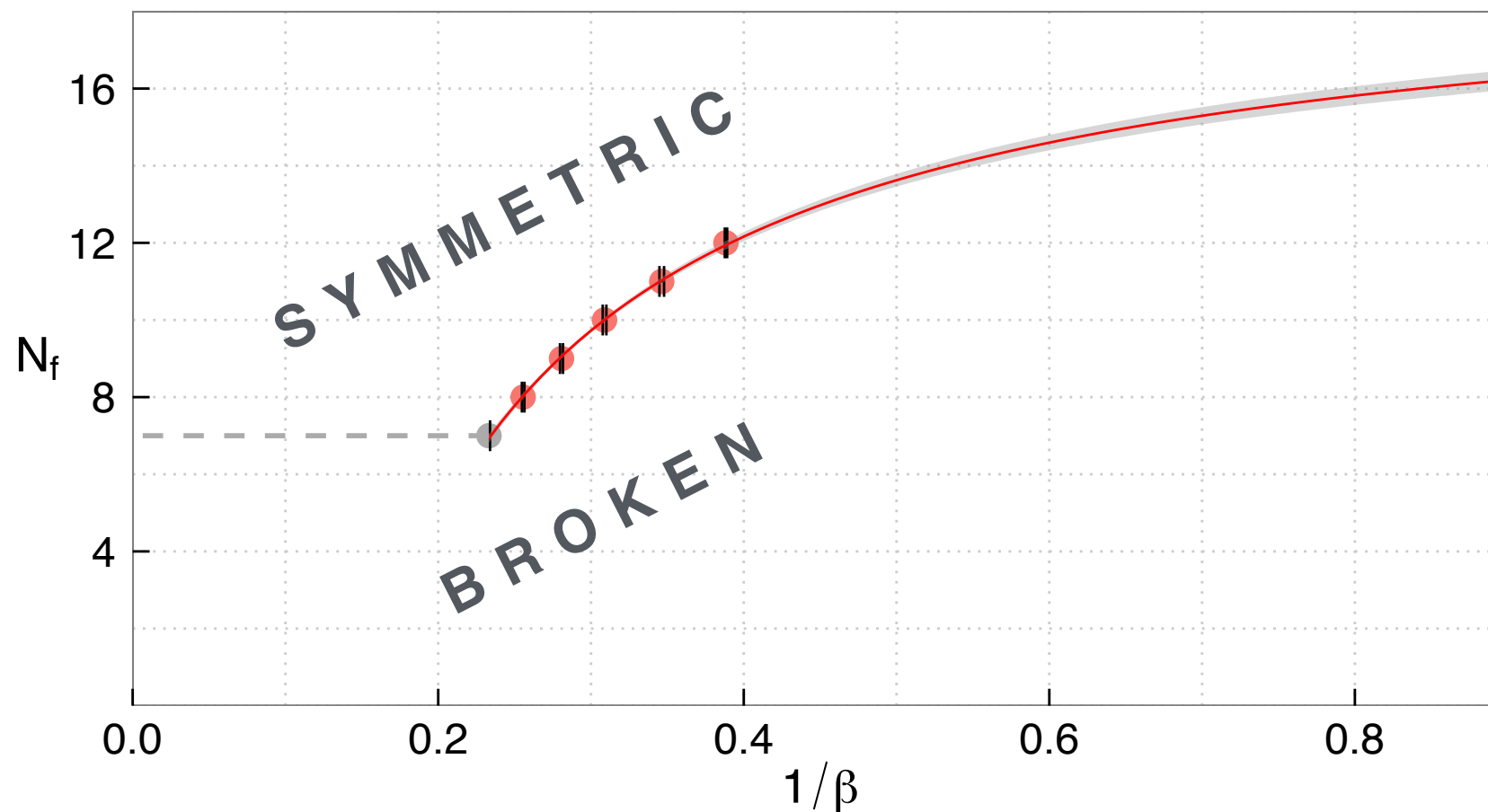
SU(3) + N<sub>f</sub> in the fundamental

Order parameter of chiral symmetry breaking (χSB)

(Chiral symmetry restored if conformal symmetry realized)

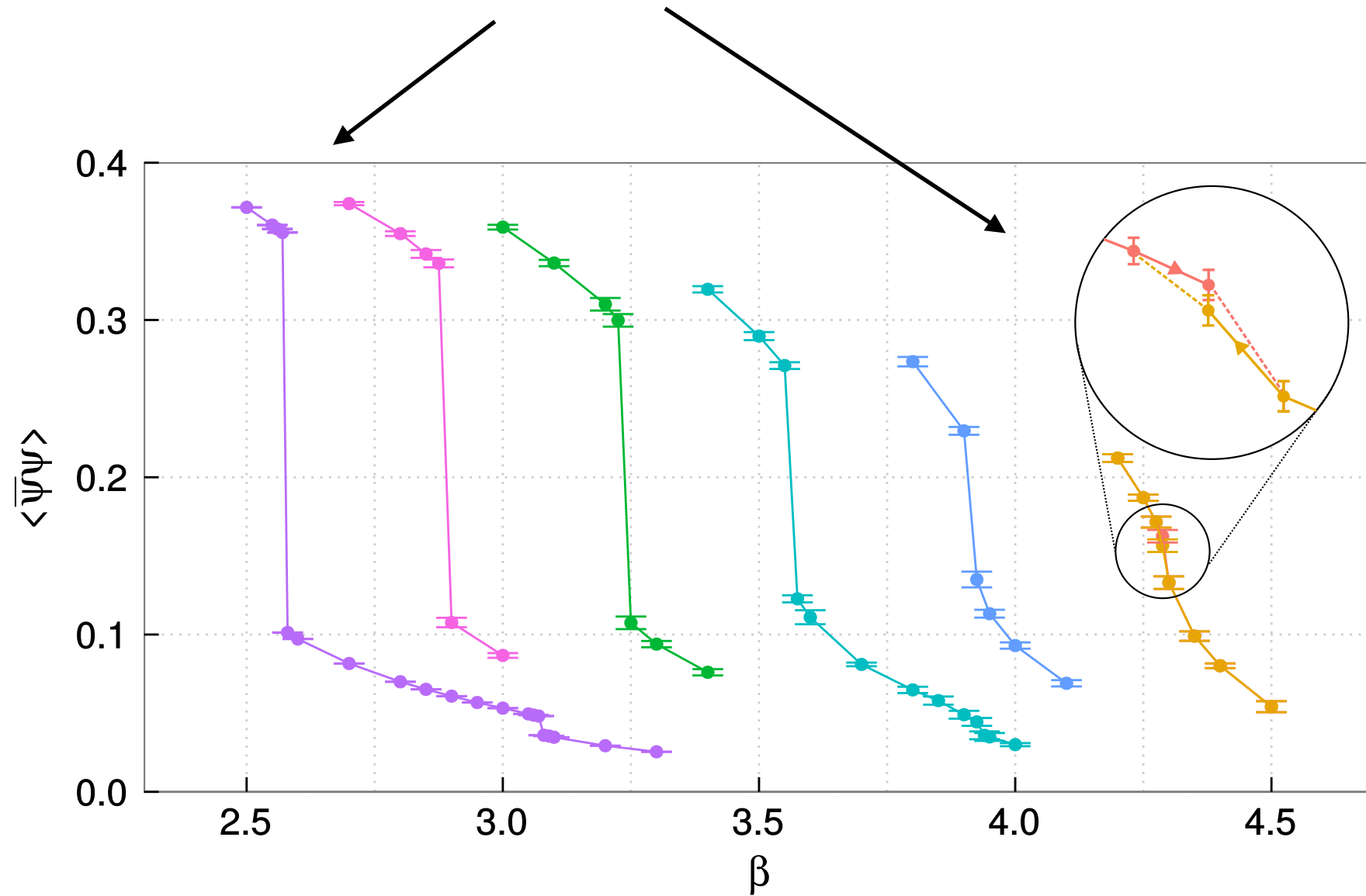
Line of bulk ( $T=0$ ) chiral symmetry breaking phase transitions for  $N_f \searrow N_f^c$

[ARXIV:1506.06396]



The  $N_f$  dependence of the line is a leading order effect separating phases with different symmetries: larger  $N_f$  implies enhanced screening

Sequence  $N_f = 12, \dots, 7$  :  $am=0.01$   $V=16c32, 12c24$



NB: Exotic phase does not touch chiral symmetry (edge displayed for  $N_f=12, 9$ )  
Expected to merge with bulk line at the endpoint in the massless limit.



# Interpretation

Results consistent with a lower edge below  $N_f = 8$  and close to  $N_f = 7$

- ▶ Not far from two-loop perturbation theory  $N_f^c \gtrsim 8$
- ▶ In better agreement with four-loop perturbation theory  $7 < N_f^c < 8$
- ▶ Remarkably, in agreement with large- $N$  QCD in the Veneziano limit

Lower edge at  $N_f/N = 5/2$  [BOCHICCHIO 2013 ARXIV:1312.1350]

where quantum instability of glueball kinetic term sets in

**NB agreement between an observable sensitive to confinement and an observable sensitive to chiral symmetry breaking**

Scalar glueball operator  
anomalous dimension

## Trace anomaly of QCD

$$T_{\mu}^{\mu} = \frac{\beta(\alpha)}{16\pi\alpha^2} \text{Tr}(G^2) + \text{fermion mass contribution}$$

$$\beta(\alpha) \equiv \frac{d\alpha(\mu)}{d \ln \mu} \quad \alpha \equiv \frac{g^2}{4\pi}$$

## Scaling of a quantum operator

$$\frac{dO}{d \ln \mu} = d_O O \quad O(\mu) \sim \mu^{d_O} \quad d_O = d_c + \gamma_O$$

Non renormalization of  $T_{\mu}^{\mu}$  implies  $d_{T_{\mu}^{\mu}} = 4$  in  $d = 4$

$$d_G = 4 - \beta'(\alpha) + \frac{2}{\alpha}\beta(\alpha)$$

$$\gamma_G = -\beta'(\alpha^*) \quad \text{IRFP}$$



## Perturbation Theory

	$n = 2$		$n = 3$		$n = 4$	
$N_f$	$\alpha_{\text{IR},n}$	$\beta'(\alpha_{\text{IR},n})$	$\alpha_{\text{IR},n}$	$\beta'(\alpha_{\text{IR},n})$	$\alpha_{\text{IR},n}$	$\beta'(\alpha_{\text{IR},n})$
6	-	-	12.992	84.646	-	-
7	-	-	2.453	5.956	-	-
8	-	-	1.464	2.654	1.552	1.784
9	5.237	4.169	1.027	1.472	1.070	1.460
10	2.21	1.522	0.764	0.869	0.815	0.851
11	1.23	0.706	0.578	0.513	0.626	0.496
12	0.754	0.360	0.435	0.296	0.470	0.281

Two loops:  $\alpha_{\text{IR},2} = -b_1/b_2$      $\beta'(\alpha_{\text{IR},2}) = -b_1^2/b_2$

Endpoint zero\* is where  $b_2$  changes sign, i.e.,  $\alpha_{\text{IR},2} \rightarrow \infty$

\* Zero is necessary but not sufficient condition

Compare with large-N QCD beta-function in the Veneziano limit

[ BOCHICCHIO '13 ]

$$\beta(g) = \frac{g^3 c(g)}{1 - \frac{4}{(4\pi)^2} g^2}$$

—————→ zero  
—————→ pole

$c(g)$  contains an anomalous dimension term not present in SQCD

Condition for zero at endpoint is renormalisation scheme independent

What is the fate of the IRFP at the lower edge of the conformal window?  
(RG point of view)

## Plausible picture

SQCD	$N_c + 2 \leq N_f \leq 3N_c/2$ free magnetic phase	cusp in RG flow may occur
QCD	no such phase	no cusp (differentiable flow)

It also suggests that the two-loop singularity ( $b_2=0$ ) is an artifact of n-loop truncated perturbation theory.

## Fate of IRFP coupling

[LUESCHER WEISZ 02  
LUESCHER WEISZ 04  
BOCHICCHIO 13]

Learn from (large-N) Yang-Mills:

A RG scheme should exist where the coupling saturates

$$V(r) = \sigma r - \frac{g_{phys}^2(1/r)}{4\pi r}$$



breaks conformal symmetry

Zeros in a beta-function can occur also below the conformal window

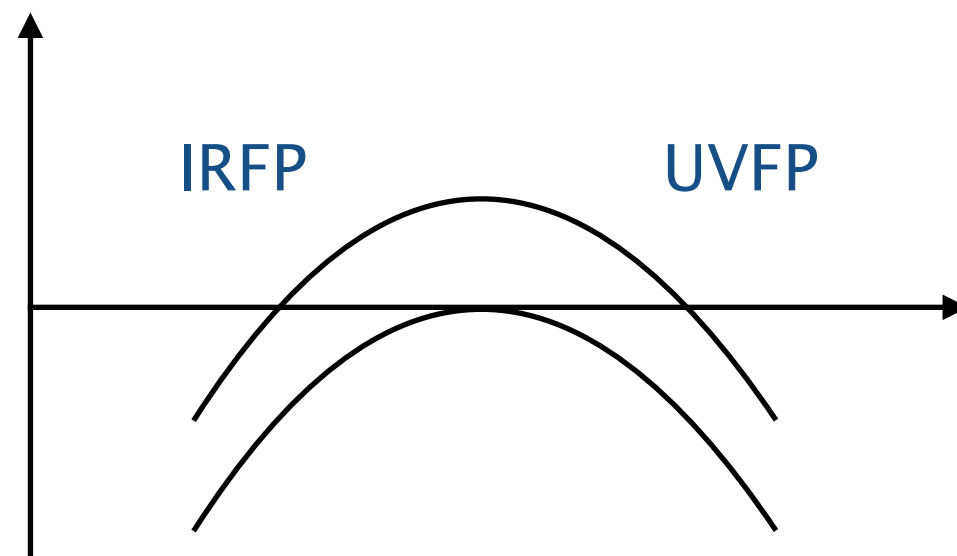


Fate of the anomalous dimension for  $N_f \searrow N_f^c$

- ▶ Perturbation theory predicts an increasing  $|\gamma_G|$  ( $|\beta'(\alpha_*)|$ )
- ▶ The large-N QCD beta-function in the Veneziano limit reproduces the two-loop result up to  $O(1/N^2)$ , but plausibly cures singularities.

UV-IR fixed point merging  
and  $\gamma G$

$$\beta(\alpha, N_f) = (N_f - N_f^c) - (\alpha - \alpha^c)^2$$



[KAPLAN ET AL 2009]

$$\beta'(\alpha^c) = 0, \quad \text{a local maximum at } N_f^c$$

Its magnitude decreases for  $N_f \searrow N_f^c$

# Conclusions I

- ▶ A numerical study of the chiral properties of QCD is consistent with the lower edge of the conformal window below  $N_f=8$  and close to  $N_f=7$
- ▶ This is in agreement with perturbation theory and, remarkably, with a recent large- $N$ +Veneziano limit prediction based on the properties of glueball dynamics
- ▶ In the end the complete theory may just be close to perturbation theory and large- $N$ .



# Conclusions II

- ▶ Best observables to probe the lower edge:
  - n-point functions sensitive to string tension (confinement)
  - n-point functions sensitive to chiral symmetry
  - topological quantities
- ▶ The scalar glueball anomalous dimension discriminates between different mechanisms for the loss of conformality